



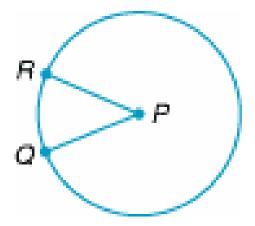
Green weight weight weight weight

Last week we learned how to find the degree *measure* of an arc of a circle—it was the same as the degree measure of the intercepted central angle.

For instance, in this circle, in $\odot P$, if $\overline{PR} = 9in$, $m \angle QPR = 40$, then $m\widehat{QR} = 40$ too.

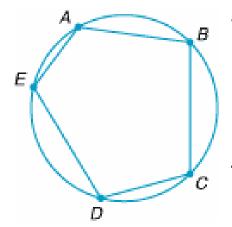
The arc length, s, measured in a linear unit, is a part of the circumference that is proportional to the measure of the central angle compared to the entire circle.

$$\frac{part \text{ of circumference}}{whole \text{ circumference}} = \frac{\text{degree } part \text{ of circle}}{\text{degree of } whole \text{ circle}}$$
$$\frac{arc \text{ length}}{2\pi r} = \frac{central \text{ angle}}{360^{\circ}}$$



Given a circle, we can inscribe either a polygon or an angle inside of it.

A polygon is said to be inscribed if each of its



vertices lies on the circle. For instance, polygon ABCDE is an inscribed pentagon. The line segments are chords.

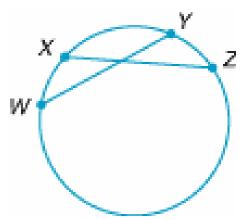
Notice that an arc can be defined, not only by a central angle, but also by a chord.

Here's an important theorem relating two minor arcs to their respective chords.

Theorem: In a circle (or congruent circles), two or more arcs are congruent if and only if their corresponding chords are congruent.

Example:

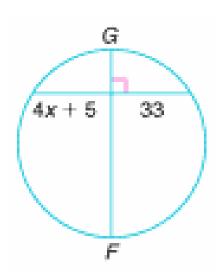
In the circle, $\widehat{mWX} = 30$, $\widehat{mXY} = 50$, $\widehat{mYZ} = 30$, and $\widehat{WY} = 14$. Find XZ.



Here's another important theorem relating a circle's diameter to a special chord.

Theorem: If a diameter is perpendicular to a chord, then it bisects the chord and its arc.

Example:

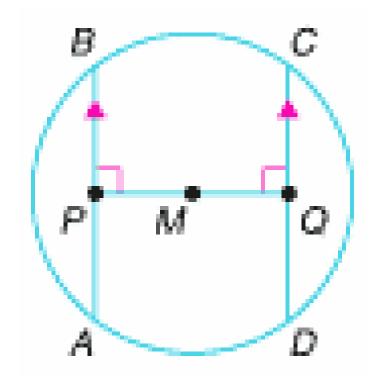


If \overline{GF} is a diameter of the circle, find the value of x.

Theorem: Two chords are congruent if and only if they are equidistant from the center.

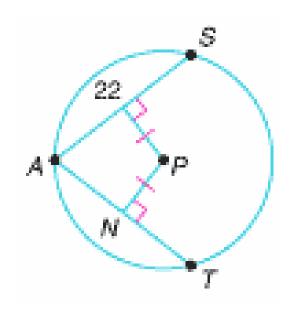
Example:

In $\bigcirc M$, $\overline{AB} \parallel \overline{CD}$, and $\overline{AB} \cong \overline{CD}$. If MP = 3, and CD = 8, what is the radius of the circle?



Example:

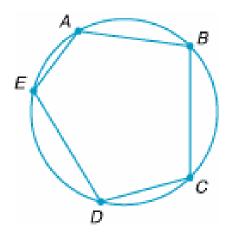
Find NT



Angles can also be inscribed in a circle.

An inscribed angle has its vertex on the circle and its two sides are chords of a circle.

All of the angles in this inscribed pentagon are also inscribed angles. For instance, $\angle EAB$ or $\angle BCD$ are inscribe angles.



Each inscribed angle has an intercepted arc. For example, the intercepted arc of $\angle EAB$ is \widehat{EDB} or \widehat{ECB} .

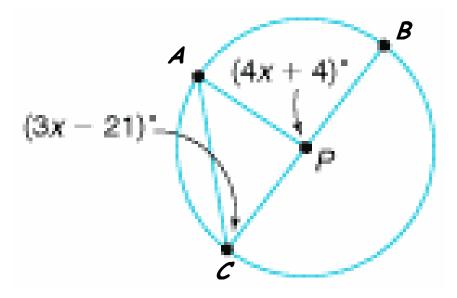
Can we tell anything about the intercepted arc from its corresponding inscribed angle?? But of course . . .

If an angle is inscribed in a circle, then the measure of the angle equals one-half the measure of the intercepted arc (or the arc's measure is twice the angle's measure).

Example:

If P is the center of the circle, find the value of

X.

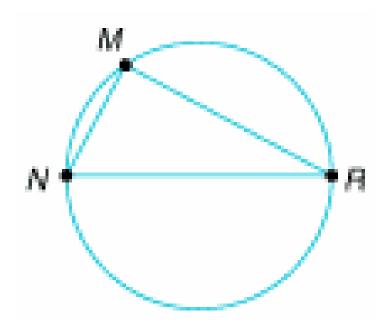


One last important theorem for today.

Theorem: If an inscribed angle of a circle intercepts a semicircle, then the angle is a right angle.

Example:

If \overline{NR} is a diameter of the circle, MR = 12, and the circle has radius 10, then find NM.



ीका प्राविध्या

The Area, A, of a circle is a measure of how much space it takes up in a plane. Its formula is given by the following:

$$A = \pi r^2$$

We have used this formula several times on previous episodes, but where did it come from? Do these things fall from the sky? Do they grow on trees? Guess who discovered it

ARCHIMEDES

Here's the real story behind his inspiration:

One sunny afternoon, Kyle and Wendy, two ancient toga tailors, asked Archimedes if he was interested in walking down to a very popular pizza parlor in downtown Syracuse, Sicily for lunch. Kyle and Wendy wanted to repay Archimedes for his kindness in helping them develop a lightweight, yet durable, toga material that left the wearer cool in the summer and warm in the winter. Even though Archimedes was extremely busy, he did not want to upset his friends so he accepted their lunch invitation.



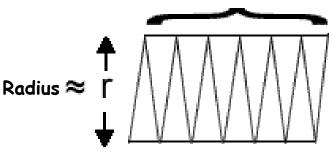
They place an order for a large, 14-inch round pizza, but just as it was served, Kyle and Wendy get summoned on a Toga service call: *Toga emergency*. They immediately jump from their seats to answer the call for comfort, leaving Archimedes alone with the pizza.

Not interested in service calls and not really hungry, Archimedes calls to the chef, "Hey, Rosseti, bringa me a biga, sharpa knife!" Not understanding why Archimedes wants the knife, the chef obliges, and watches in horror while Archimedes begins to cut the round pizza into very thin slices. Each slice of pizza was uniform in size and the slices were even in number.



Now, for every slice, there is a "*Top*" and a "*Bottom*". Placing a top and bottom together, side by side, Archimedes discovered the circle becomes rectangular. The area of the near rectangular shape is approximately





$$(\pi r)(r) = \pi r^2$$
Voilà!

Resources:

www.glencoe.com

http://www.worsleyschool.net/science/files/circle/area.html