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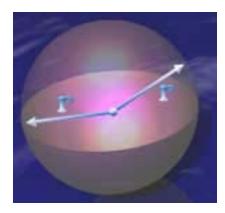
Today we look at the fascinating sphere.

Of all the shapes, a sphere has the smallest surface area for a volume. Or put another way it can contain the greatest volume for a fixed surface area.

The sphere appears in nature whenever a surface wants to be as small as possible. Bubbles and water drops, for example

Here are some other interesting things to notice about spheres:

- It is perfectly symmetrical
- It has no edges or vertices
- It is **not** a polyhedron
- All points on the surface are the same distance from the center



Here's some terminology:

A great circle is a circle on the sphere that has the same center and radius as the sphere, and consequently divides it into two equal parts. The shortest distance between two distinct non-polar points on the surface and measured along the surface, is on the unique great circle passing through the two points.

If a particular point on a sphere is designated as its <u>north pole</u>, then the corresponding antipodal point is called the <u>south pole</u> and the <u>equator</u> is

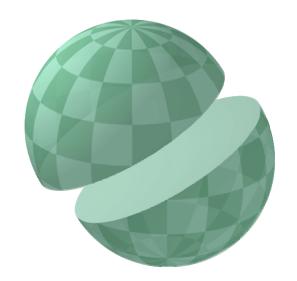
the great circle that is equidistant to them.

Great circles through the two poles are called lines (or meridians) of longitude, and the line connecting the two poles is called the axis of rotation.

Circles on the sphere that are parallel to the

equator are lines of <u>latitude</u>. This terminology is also used for astronomical bodies such as the planet <u>Earth</u>, even though it is actually a <u>geoid</u>.





A sphere is divided into two equal hemispheres by any plane that passes through its center.

Now let's look at two formulas for Spheres that will help us find some important quantities.

The Surface Area of a Sphere with radius r is given by

$$SA = 4\pi r^2$$

The Volume of a Sphere is given by

$$V = \frac{4}{3}\pi r^3$$

Notice that there are only two variable in each equation. Remember $\pi \approx 3.14159...$

If we know the radius, we can find the surface area or volume.

If we know the surface area or volume, we can find the radius.

You will have several types of problems. The first is when you are given the radius. These will be "plug-and-chug" varieties.

Example:

You and your friends are on Spring Break playing with a beach ball. Your "mathy" friend asks, "Hey, how much vinyl makes up this ball, and how much air is inside?" Your friend is simply inquiring about the sphere's surface area and volume, respectively.

Let's assume the ball's diameter is 3 feet.



http://www.cistyles.com/forms.htm

Sometimes you may need to find the radius when given either the volume or surface area. Remember these equations are really formulas or literal equations and can be used in any equivalent form.

http://www.nutratechinc.com/advz/

Example:

After a game of beach ball, Jenna replenishes her electrolytes by peeling and eating a

delicious orange. When she is done, relaxing in the cool spring breeze, she calculates the amount of orange peeling from her snack to be roughly 80 square inches. Now she wants to know what the radius of her orange was!

Mr. Korpi, 2006-2007

Now the problems get more interesting when you are given neither the radius, diameter, surface area, OR the volume, but instead some other quantity. In this case, you will have to extract the needed information, essentially squeezing your own orange juice.

Example:

Find the volume of a sphere whose great circle has a circumference of 31.4 in.

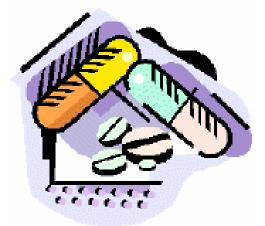
Here's one that requires a bit more work (so obtaining its result will be more satisfying)!

Example:

Find the volume of a sphere with a surface area of 615.8 in².

Sometimes the calculations require a little ingenuity and a combination of formulas.

Example:



A pharmacist is filling medicine capsules. The capsules are cylinders with half spheres on each end. If the length of the capsule is 16 mm and the radius is 2 mm,

how many cubic mm of medication can one capsule hold?

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Archimedes part |

Eureka Moment

The tyrant Hiero of Syracuse once approached Archimedes seeking a solution to an unusual puzzle:

Having commissioned an artisan to produce a crown, Hiero had given the man some gold. When the



crown was complete, Hiero suspected the gold



King Hiero

had been mixed with silver (a less expensive metal), enabling the artisan to quietly pocket the difference. Was there, Hiero wondered, any way to put his suspicions to the test?

According to the traditional tale, the answer occurred to Archimedes while he was bathing; he noticed that as he immersed himself in the tub, not only did the water level rise, but his apparent weight seemed to decrease.

He is said to have leaped from the bath and run naked through the streets of



Syracuse crying, "Eureka! Eureka!" (I have found it! I have found it!)

Here's a related example:

Seven steel balls, each of diameter 4cm, are dropped into a tall cylinder tank of radius 5cm, which contains water. By how much does the water level rise? (Assume the balls are entirely submerged.)

 By the Archimedean principle of fluid buoyancy, the balls displace an equal volume of water, so it will rise x cm.

• Vol. of 7 balls=
$$7\left[\frac{4}{3}\pi(2^3)\right] = \frac{224\pi}{3} cm^3$$

• Increase in vol. Of water= $\pi r^2 x = \pi (5)^2 x = 25\pi x$

Setting the two volumes equal,

$$\frac{224\pi}{3} = 25\pi x$$

$$x = \frac{224\pi}{3(25\pi)} = \frac{224}{75} \approx 2.987$$
 cm

So, The water level rises about 3 centimeters.

Resources:

www.glencoe.com

http://en.wikipedia.org/wiki/Sphere