Name

Date

Period

Worksheet 5.5—Application of Sinusoids

Show all work on a separate sheet of paper. A calculator is permitted. Report three decimals and units in all final answers.

Multiple Choice

- 1. The height, h, in meters, above the ground of a car as a Ferris Wheel rotates can be modeled by the function $h(t) = 16\cos\left(\frac{\pi t}{120}\right) + 18$, where t is the time, in seconds. $|A| = 1/\varphi$
 - I. What is the radius of the Ferris Wheel?

(A) 18 m

(B) 8 m



(D) 9 m

(E) 2 m

II. What is the maximum height of the car?

(A) 18 m

(B) $26 \, \text{m}$

(C) 16 m

(D) 17 m (E) 34 m 16 + 18

III. How long does it take for the wheel to make one revolution?

(A) 120 s (B) $\frac{\pi}{120}$ s (C) 240 s

lution? (D) $\frac{120}{\pi}$ s (E) 60 s $P = \frac{2\pi}{120} (t) + 18$

IV. What is the minimum height of the car?

(B) 4 m

(C) 16 m

V. How fast does the wheel rotate?

(A) 120 rad/s

| rad/s

(C) 240 rad/s

(D) $\frac{\pi}{240}$ rad/s (E) $\frac{120}{\pi}$ rad/s

- 2. Another Ferris Wheel at another amusement park has riders get on at position A, which is 3 meters above ground. The highest point of the ride is 15 m above the ground. The ride takes 40 seconds for one complete revolution.
 - I. An equation modeling the height of a rider over time for this Ferris Wheel is

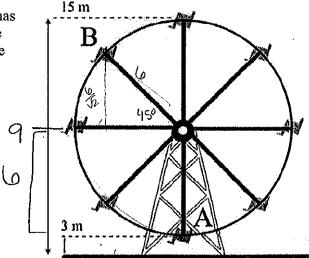
(A)
$$h(t) = -6\cos 9t + 9$$

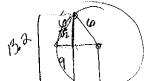
(B)
$$h(t) = -6\cos 40\pi t + 9$$

(C)
$$h(t) = -6\cos\frac{\pi t}{3} + 9$$

(E)
$$h(t) = -6\cos\frac{\pi t}{20} + 9$$
 $P = 40$
(E) $h(t) = -6\cos\frac{\pi t}{40} + 9$ $P = 40$



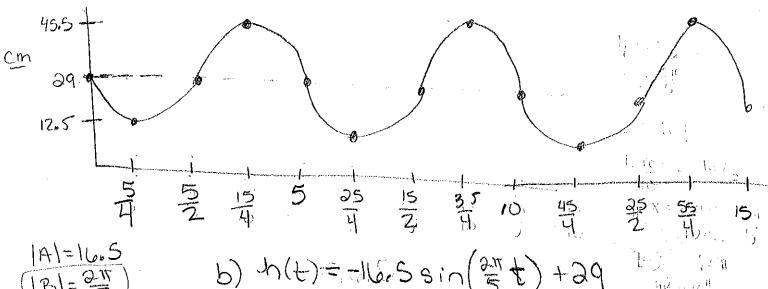




- II. The time it takes for a rider, who starts at position A, to travel to position B (a rotation of 135°) is
 - (A) 12 s
- (B) 13 s
- (C) 14 s
- (D) 15 s
- (E) 16 s (h(t) = 14.936
- 10,709 soc X3 III. If the ride makes three complete rotations, the total amount of time a rider on the Ferris Wheel will spend above 13 m, rounded to the nearest second, is (E) 45 s(A) 11 s(B) 15 s(C) 25 s(D) B2 s
- - IV. If the Ferris Wheel rotates counter-clockwise, instead of the original clockwise motion, the new equation can be represented by
 - (A) applying the transformation y = -h(t)
 - (B) applying the transformation y = h(t-20)
 - (C) applying the transformation y = h(-t)
 - (D) applying the transformation y = -h(-t)
 - (E) using a sine function instead of a cosine function, with no change to the parameters

Free Response

- 3. The pedals of a bicycle are mounted on a bracket whose center is 29 cm above the ground. Each pedal is 16.5 cm from the center of the bracket. Assume that the bicycle is pedaled at 12 revolutions per minute. With the starting position of the pedal in a horizontal position at t = 0 seconds.
 - (a) Sketch the graph of this sinusoidal function of the height of one pedal in cm (with respect to seconds) for the first three cycles. Label and number the axes appropriately.
 - (b) Write an equation for this function expressing the height y as a function of time t.
 - (c) When is the pedal 40 cm above the ground for the first time?
 - (d) How high is the pedal after 23 seconds? At this time, is the pedal going up or down?



c)
$$h(t)=40$$

 $t=3.080$ sec.

d) 38,698 cm above the ground going up.

4. The center of a bicycle wheel is 33 cm above the ground. A reflector mounted on the spokes is located 17.5 cm from the center of the wheel that is turning at a constant rate of one revolution per second. If y is the height of the reflector in cm, and t represents the time in seconds;

(a) What is the amplitude of the reflector?

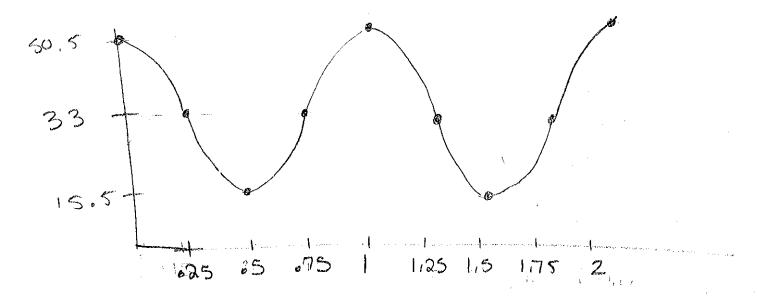
- (b) What is the period? How many rotations does the reflector make in 2π seconds?
- (c) If at $t = \frac{3}{4}$ seconds, the reflector is 33 cm above ground and moving up, what is the equation representing height of the reflector above ground in cm as a function of time in seconds?

(d) Sketch and label this sinusoidal graph for two complete revolutions.

(e) How high was the reflector when the bicycle first started moving at t = 0? At his time, was the reflector moving up or down?

(f) At what time does the reflector first pass through a height of 25cm above the ground?

(g) How would the equation change if the reflector was in a position 2 cm further from the center of the wheel?



$$e) f(0) = 50.5$$

L=.327 sec.

9) / Alwould be two units larger

- 5. The depth of water at the end of a pier varies with the tides throughout the day. Today the high tide occurs at 4:15 a.m. with a depth of 5.2 m. The low tide occurs at 10:27 a.m. with a depth of 2.0 m.
 - (a) Sketch a graph showing how the depth of the water depends on the time since midnight.
 - (b) Find a trigonometric equation that models the depth of the water t hours after midnight.
 - (c) Find the depth of the water at noon.
 - (d) A large boat needs at least 3 m of water to moor at the end of the pier. During what time period after noon can it safely moor?

