Name___

Worksheet 1.1—Exponents

No Calculator

I. Multiple Choice: Show all work on MC questions. No work, No credit.

- _____1. Which of the following is equivalent to $x^{3/4}$?
 - (A) $\frac{1}{x^{4/3}}$ (B) $x^{-4/3}$ (C) $x^{4/3}$ (D) $\sqrt[3]{x^4}$ (E) $\sqrt[4]{x^3}$

_____2. What is the value of $\left(-\frac{1}{2}\right)^{-4}$?

- (A) 16 (B) 2 (C) 8 (D) -8 (E) -16

_____ 3. Which of the following is the simplified form of $\frac{x^6}{x^{-2}}$, $x \ne 0$?

- (A) x^{-4} (B) x^2 (C) x^3 (D) x^4 (E) x^8

_____4. Simplify $\left(-3x^2y^5\right)^{-4}$ using only positive exponents.

- (A) $81x^8y^{20}$ (B) $\frac{x^8y^{20}}{81}$ (C) $\frac{1}{81x^8y^{20}}$ (D) $\frac{-1}{81x^8y^{20}}$ (E) $\frac{81}{x^8y^{20}}$

___ 5. Evaluate $-625^{1/4}$

- (A) -5 (B) 5 (C) $-\frac{1}{5}$ (D) $\frac{1}{5}$ (E) DNE, "Does Not Exist"

_____ 6. Evaluate $\left(\frac{36}{25}\right)^{-3/2}$

- (A) $\frac{6}{5}$ (B) $\frac{125}{216}$ (C) $\frac{216}{125}$ (D) $\frac{5}{6}$ (E) $-\frac{216}{125}$

_____ 7. If x = -2 and y = -3, what is the value of the expression $\frac{c^x}{c^y} - \frac{c^y}{c^x}$, for $c \ne 0$.

- (A) 0 (B) $\frac{c^2+1}{c}$ (C) 2c (D) $\frac{c^2-1}{c}$ (E) $\frac{c}{1-c^2}$

_____8. The expression $\frac{3^{1/3}}{3^{-2/3}}$ is equivalent to which of the following?

- (A) 1 (B) 3 (C) $\sqrt{3}$ (D) $\frac{1}{\sqrt[3]{3}}$ (E) $\frac{1}{\sqrt{3}}$

II. Short answer

9. Find any and all mistakes, explain what they are, then work the problem correctly

(a)
$$\left(-4ab^5\right)^7 = -28a^7b^{12}$$

(b)
$$(3x^2y^{1/2})(7x^{10}y^8) = -21x^{20}y^4$$

10. Simplify each the expressions as much as possible (if possible). For each term, you should have only one representative factor of each type. Practice writing your final answer without any fractional or negative exponents.

(a)
$$\frac{\left(x^{-3}y^2\right)^{-4}}{\left(\sqrt{y^6}x^{-4}\right)^{-2}}$$

(b)
$$\left(\frac{4a^3b}{\sqrt[3]{a^2b^3}}\right) \left(\frac{2a^2b^4}{3b^2}\right)^{-1}$$

(c)
$$2x^4y^{-3}x^{-19} + y^{\frac{1}{3}}y^{-\frac{3}{4}}$$

(d)
$$\frac{x^{\frac{3}{5}}x^2x^{-\frac{1}{2}}}{x^{\frac{1}{10}}}$$

(e)
$$\left(\frac{2x^{-2}x^{\frac{4}{5}}y^{6}}{x+y}\right)^{-3}$$

(f)
$$\frac{x^2y^{-3} \cdot \sqrt{9\sqrt{x^{-3}\sqrt{y^5}}}}{\sqrt{x^3y^5}}$$

11. Provide a counterexample for the claim that $\sqrt{a^2 + b^2} = a + b$. Clearly define you values and show your work.