TEST: 5.1-5.5—Calculator Permitted

Part I: Multiple Choice

1. What is the period of the following sinusoid: $y = 5 - 3\cos\left(\frac{2\pi}{3} + \frac{4\pi}{3}x\right)$?

(A)
$$\frac{2\pi}{3}$$

(A)
$$\frac{2\pi}{3}$$
 (B) $\frac{4\pi}{3}$ (C) $\frac{3}{2}$

(C)
$$\frac{3}{2}$$

(E) 3

_____2. Which of the following angles is coterminal with $\frac{447/35\pi}{7}$?

(A)
$$\frac{3\pi}{7}$$
 (B) $\frac{5\pi}{7}$ (C) $\frac{9\pi}{7}$ (D) $\frac{11\pi}{7}$ (E) π

(B)
$$\frac{5\pi}{7}$$

(C)
$$\frac{9\pi}{7}$$

(D)
$$\frac{11\pi}{7}$$

3. Which of the following is equal to $\sec^{-1} 0.5$?

(B) 0.016

(D) 1.139

(E) undefined

___4. For $\theta = -16115123.2^{\circ}$, Find the reference angle, θ_{ref}

(A)
$$6.798^{\circ}$$

$$(C) -83.202^{\circ}$$

(D)
$$-6.798^{\circ}$$

(E) $\frac{\pi}{6}$

5. If the terminal ray of θ passes through the point (-1,-2), then $\csc \theta = ?$

$$(A) \ \frac{1}{2}$$

(A)
$$\frac{1}{2}$$
 (B) 2 (C) $-\frac{\sqrt{5}}{2}$ (D) $-\sqrt{5}$ (E) $-\frac{\sqrt{5}}{5}$

(D)
$$-\sqrt{5}$$

(E)
$$-\frac{\sqrt{5}}{5}$$

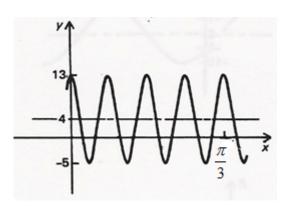
6. Approximately how many cycles will the function $f(x) = 13\sin(4\pi x) - 14$ have from 0 to 2π ?

(E) 0.25

7. For the given graph shown at right, how many cycles does it have between 0 and 2π ?

(A)
$$\frac{\pi}{3}$$

(A)
$$\frac{\pi}{3}$$
 (B) $\frac{2\pi}{3}$ (C) 24 (D) 12 (E) 36



8. Determine the range of the function

 $y = -\frac{3b}{2} + \frac{b}{2}\cos 4ax$, where a > 0, b > 0.

(A)
$$\left\{ y \middle| \frac{b}{2} \le y \le \frac{3b}{2} \right\}$$

(A)
$$\left\{ y \middle| \frac{b}{2} \le y \le \frac{3b}{2} \right\}$$
 (B) $\left\{ y \middle| -\frac{3b}{2} \le y \le -\frac{b}{2} \right\}$ (C) $\left\{ y \middle| b \le y \le 2b \right\}$

(C)
$$\{y | b \le y \le 2b\}$$

(D)
$$\{y | -2b \le y \le -b\}$$
 (E) $\{y | -b \le y \le 2b\}$

$$(E) \left\{ y \middle| -b \le y \le 2b \right\}$$

Part II: Free Response

Show all work, including the equations your are solving/evaluating on your calculator. Give simplified, exact answers when specified, otherwise report **three decimals**. Avoid intermediate rounding error. Box your final answers, **with units** when appropriate.



Mark Twain sat on the deck of a river steamboat with his stopwatch. As the paddlewheel turned, **a point** on the outer edge of the paddlewheel moved in such a way that its distance, *d* in **feet**, from the water's surface was a sinusoidal function of time, *t* in **seconds**. When his stopwatch read 4 seconds, the point was at its highest, 16 ft above the water's surface. The wheel's diameter was 18 ft and rotates at 6 RPMs (revolutions per minute).

- (a) What is the period, in seconds, of the paddle wheel?
- (b) Sketch at least 2 cycles of the graph of the sinusoid. Be sure to label and scale both your axes. Show it crossing the *y*-axis.
- (c) Write an equation of your graph modeling the height, d(t), at time t.
- (d) Where was the point, in feet, **in relation to the water's surface** when Mark started his stopwatch? At this time, in which vertical direction was that point moving?
- (e) During the first 15 seconds from the time Mark started his watch, for how many seconds does the point remain underwater? Show the work that leads to your answer.
- (f) What is the total distance, in feet, this point on the outer edge of the paddlewheel travel in one minute?
- (g) What is the linear velocity, in feet per second, of this point?
- (h) What was the full birth name of Mark's grandfather's son's son's name?