

BC Test: Chapter 9.1, Calculator Permitted

Do your fork on this page.

1. Determine if the sequence $\left\{ \frac{100 \ln^{10} n}{n} \right\}$ converges or diverges. Show your work.

2. Determine if the following series converge or diverge. Justify using the name the test and show any calculations used to make your determination.

$$(a) \sum_{n=1}^{\infty} \sqrt{\frac{1+3n^2+n^3}{4n^3-5n+2}}$$

$$(g) \sum_{n=1}^{\infty} \frac{n^2}{5^n}$$

$$(l) \sum_{n=2}^{\infty} \frac{1}{(\ln \sqrt{n})^n}$$

$$(b) \sum_{n=1}^{\infty} \frac{\pi}{\sqrt{n^5}}$$

$$(h) \sum_{n=0}^{\infty} \left(\frac{7}{2}\right)^{-n}$$

$$(m) \sum_{n=2}^{\infty} \frac{n^2}{(2n-1)!}$$

$$(c) \sum_{n=1}^{\infty} \frac{1}{\sqrt[3]{n^5+5}}$$

$$(i) \sum_{n=1}^{\infty} \frac{4}{n^3+1}$$

$$(n) \sum_{n=1}^{\infty} \left(\frac{5n^2}{7n^2-100n} \right)^n$$

$$(d) \sum_{n=1}^{\infty} \frac{5n^2 - 6n + 3}{n^3 - 7n + 8}$$

$$(j) \sum_{n=1}^{\infty} (\sec n\pi) n^{-2/3}$$

$$(o) \sum_{n=1}^{\infty} \frac{(-10)^n}{4^{2n+1}(n+1)}$$

$$(e) \sum_{n=1}^{\infty} \frac{3^n + 4}{2^n}$$

$$(k) \sum_{n=1}^{\infty} \frac{8n^3 - 6n^5}{12n^4 - 9n^6}$$

$$(p) \sum_{n=1}^{\infty} \frac{2^{n-1}}{n(-3)^n}$$

$$(f) \sum_{n=1}^{\infty} \sqrt{\frac{3n+1}{n^5+2}}$$

3. Determine if the series $\sum_{n=5}^{\infty} \frac{(-1)^n}{\sqrt[5]{3n^7+4}}$ converges absolutely, converges conditionally, or diverges.

4. What is the sum of each of the following:

(a) $\sum_{n=3}^{\infty} \frac{2^{n-1}}{5^n}$

(b) $\sum_{n=2}^{\infty} \left(-\frac{3}{2}\right)^{-n}$

(c) $\sum_{n=1}^{\infty} \left(\frac{1}{n+1} - \frac{1}{n+4}\right)$

(d) $\sum_{n=3}^{\infty} \frac{3}{3n^2 - 12}$

5. Multiple Choice: Which of the following series converge?

I. $\sum_{n=1}^{\infty} (-1)^{n+1} \frac{1}{2n+1}$

II. $\sum_{n=1}^{\infty} \frac{1}{n} \left(\frac{3}{2}\right)^n$

III. $\sum_{n=2}^{\infty} \frac{1}{n \ln n}$

(A) I only (B) II only (C) III only (D) I and III only (E) I, II, and III

Free Response:

6. Consider the series $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{3^n}$

- (a) Show that the series is absolutely convergent.
 - (b) Calculate S_4 , then determine, for S_4 , an interval in which the sum of the series resides. Round your answer to five decimal places.
 - (c) Find the number of terms necessary to approximate the sum of the series with an error less than 0.0001
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