5. The function $f(x) = x^{-1/9}$ has how many inflection points?
(A) 0
(B) 1 (C) 2
(D) 3
(E) 4
6. The function $f(x) = x^4 - 8x^3$ has
(A) A relative maximum at $x = 0$; no relative minimum
(B) No relative maximum; a relative minimum at $x = 6$
(C) A relative maximum at $x = 0$; a relative minimum at $x = 6$ (D) A relative maximum at $x = 0$; a relative minimum at $x = -6$ and $x = 6$
(E) A relative minimum at $x = 0$; a relative maximum at $x = -6$.
7. Using the linearization of $f(x) = \sqrt[3]{x}$ at $x = 64$, how much less that 4 is the value of $\sqrt[3]{63}$?
(A) $\frac{1}{48}$
(B) $\frac{1}{16}$
(C) $\frac{1}{3}$
(D) $\frac{2}{3}$
(E) 1
8. If f is differentiable, we can use the line tangent to $f(x)$ at $x = c$ to approximate values of $f(x)$
near $x = c$. Suppose this method always underestimates the correct values. If so, in the neighborhood of $x = c$, f must be
(A) positive
(B) increasing
(C) decreasing
(D) concave up (E) concave down
(L) concave down
9. The length of a happy rectangle is increasing at 3 times the rate that its width is increasing. When the length is 12 feet and the width is 6 feet, the diagonal of the happy rectangle is increasing how many
times faster that the width?
$(A) \frac{7}{\sqrt{5}}$
(B) $7\sqrt{5}$
(C) $\frac{5}{3\sqrt{5}}$
$3\sqrt{5}$
(D) $15\sqrt{5}$
(E) $6\sqrt{5}$

- II. Free Response: Show all work in the space provided using correct notation. Include units on all final answers.
- 10. Non-alcoholic Wassail is draining at the rate of $\frac{\pi}{1000}$ ft³ / sec from the vertex the bottom of a HUGE German conical tank whose diameter at its base is 40 feet and whose height is 60 feet.



Teet and Whose height is 60 feet.	•
(a) Write an equation for the volume of the Wassail in the German tank, in cubic feet, in terms of in feet, at the surface of the Wassail.	its radius,
in rect, at the surface of the wassain.	
(b) At what rate, in feet per second, is the radius of the Wassail in the German tank changing who radius is 10 feet?	en the
radius is 10 leet!	

(c) How fast is the height of the Wassail in the German tank changing, in feet per second, at the instant that the radius is 10 feet?
(d) If a toons and unicern coloraba and an along his ordinarial common anotice. We say it 2017 may and an
(d) If a teenaged unicorn calculus scholar places his cylindrical commemorative Wassail 2017 mug under the draining Wassail in the hope to imbibe the festive non-alcoholic beverage, how fast is the height of the Wassail in the commemorative mug rising (in inches per second) when the radius of the Wassail in the German tank is 10 feet? Assume the commemorative mug has a 2-inch diameter and is 3 inches tall
with a cute, tiny little mug handle. NOTE: $\frac{\pi}{1000}$ ft ³ /sec = 1.728 π in ³ /sec