AP Calculus AB/BC

TEST: 3.1 to 3.8, Calculator OK

_____ 1. How many values of c satisfy the Mean Value Theorem for the equation $f(x) = x \cos(\sqrt{x})$, $0 \le x \le 50$?

- (A) 0
- (B) 1
- (C) 2
- (D)3
- (E) 4

____ 2. The function f is twice differentiable with f(2)=1, f'(2)=4, and f''(2)=3. What is the value of the approximation of f(1.9) using the line tangent to the graph of f at x = 2?

- (A) 0.4
- (B) 0.6
- (C) 0.7
- (D) 1.3
- (E) 1.4

3. A rectangle has one side on the x-axis and the upper two vertices on the graph of $y = e^{-2x^2}$. Give a decimal approximation for the maximum possible area for this rectangle.

- (A) 1.649
- (B) 1
- (C) 2.031
- (D) 0.545
- (E) 0.606

__ 4. Let f be the function given by $f(x) = 2xe^x$. The graph of f is concave down when

- (A) x < -2
- (B) x > -2
 - (C) x < -1
- (D) x > -1
- (E) x < 0

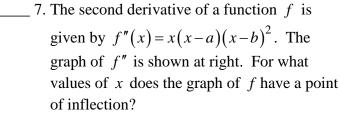
5. The radius of a sphere is decreasing at a rate of 2 centimeters per second. At the instant when the radius of the sphere is 3 centimeters, what is the rate of change, in square centimeters per second, of the surface area of the sphere?

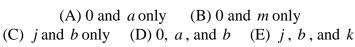
- (A) -108f
- (B) -72f
- (C) -48f (D) -24f

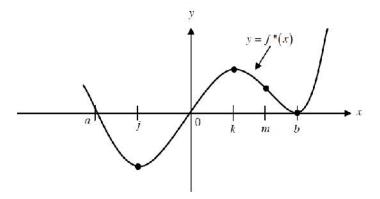
_____ 6. Let f be the function with derivative given by $f'(x) = \sin(x^2 + 1)$. How many relative extrema does f have on the interval 2 < x < 4?

- (A) One
- (B) Two
- (C) Three
- (D) Four
- (E) Five

 $_{--}$ 7. The second derivative of a function f is given by $f''(x) = x(x-a)(x-b)^2$. The graph of f'' is shown at right. For what







8. If $f(x) = 3x^2 + x$, x = 2, and dx = 0.002, find dy.

- (A) 0.02
- (B) 0.026
- (C) 0.028
- (D) 0.014
- (E) 0.26

Part II: Free Response. Do all work below the line. Label each part. Notation, Notation.

- 10. (1984-AB5) The volume V of a cone is increasing at the rate of 28f cubic inches per second. At the instant when the radius r on the cone is 3 inches, its volume is 12f cubic inches, and the radius is increasing at $\frac{1}{2}$ inches per second.
- (a) At the instant when the radius of the cone is 3 inches, what is the rate of change of the area of the base?
- (b) At the instant when the radius of the cone is 3 inches, what is the rate of change of its height h?
- (c) At the instant when the radius of the cone is 3 inches, what is the instantaneous rate of change of the area of its base with respect to its height h?

1973 AB 6

A manufacturer finds it costs him $x^2 + 5x + 7$ dollars to produce x tons of an item. At production levels above 3 tons, he must hire additional workers, and his costs increase by 3(x - 3) dollars on his total production. If the price he receives is \$13 per ton regardless of how much he manufactures and if he has a plant capacity of 10 tons, what level of output maximizes his profits?

1976 AB 4

- a. A point moves on the hyperbola $3x^2 y^2 = 23$ so that its y-coordinate is increasing at a constant rate of 4 units per second. How fast is the x-coordinate changing when x = 4?
- b. For what values of k will the line 2x + 9y + k = 0 be normal to the hyperbola $3x^2 y^2 = 23$?

1982 AB 4

A ladder 15 feet long is leaning against a building so that the end X is on level ground and end Y is on the wall. X is moved away from the building at the constant rate of $\frac{1}{2}$ foot per second.

- a. Find the rate in feet per second at which the length OY is changing when X is 9 feet from the building.
- b. Find the rate of change in square feet per second of the area of the triangle XOY when X is 9 feet from the building.