Calculus Maximus

Date\_\_\_\_\_Period\_\_\_\_

## Worksheet 9.3—Power Series: Taylor and Maclaurin Series

Show all work. No calculator except unless specifically stated.

On problems 1-3, find a Taylor series for f(x) centered at the given value of a. Give the first four nonzero terms and the general term for each series.

1. 
$$f(x) = e^{2x}$$
,  $a = 3$ 

2. 
$$f(x) = \frac{1}{x}$$
,  $a = 1$ 

3. 
$$f(x) = \ln x$$
,  $a = 1$ 

On problems 4-5, find a Taylor series for f(x) centered at the given value of a. Give the first four nonzero terms.

4. 
$$f(x) = \sin x$$
,  $a = \frac{\pi}{6}$ 

5. 
$$f(x) = \cos x$$
,  $a = -\frac{\pi}{4}$ 

On problems 6-10, find a Maclaurin series for f(x). Give the first four nonzero terms and the general term for each series. Hint: Don't reinvent the wheel (or the series), rather, modify an existing power series.

$$6. \quad f(x) = e^{\frac{-x}{2}}$$

$$7. \quad f(x) = \sin\left(x^2\right)$$

7. 
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 8.  $f(x) = \frac{\cos(3x)}{x}$  9.  $f(x) = x^2 e^{-x}$ 

9. 
$$f(x) = x^2 e^{-x}$$

10.  $f(x) = \sin^2 x$  (ADDITIONAL HINT: use the power-reducing identity)

11. (Calculator Permitted) Use your answer for problem 7 to approximate  $\int_0^1 \sin(x^2) dx$  correct to three decimal places.

12. (a) Find the first four nonzero terms in the Taylor series expansion about (centered at) x = 0 for  $f(x) = \sqrt{1+x}$ .

(b) Use the results found in part (a) to find the first four nonzero terms in the Taylor series expansion about x = 0 for  $g(x) = \sqrt{1 + x^3}$ .

(c) Find the first four nonzero terms in the Taylor series expansion about x = 0 for the function h such that  $h'(x) = \sqrt{1 + x^3}$  and h(0) = 4.

- 13. Let *f* be the function defined by  $f(x) = \frac{1}{x-1}$ .
  - (a) Write the first four terms and the general term of the Taylor series expansion of f(x) about x = 2.

(b) Use the result from part (a) to find the first four terms and the general term of the series expansion about x = 2 for  $\ln |x-1|$