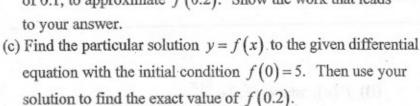
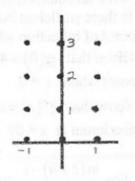
AP REVIEW 3

Work these on notebook paper (except for 1(a)). No calculator.

- 25. Consider the differential equation given by $\frac{dy}{dx} = xy$.
- (a) On the axes provided, sketch a slope field for the given differential equation at the 12 points indicated.
- (b) Let y = f(x) be the particular solution to the given differential equation with the initial condition f(0) = 5. Use Euler's method starting at x = 0, with a step size of 0.1, to approximate f(0.2). Show the work that leads to your answer.

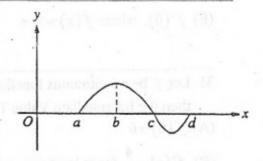




26. The graph of f is shown in the figure on the right. If $g(x) = \int_{a}^{x} f(t) dt$, for what value of x does g(x)have a maximum?

(B) b (C) c (D) d (A) a

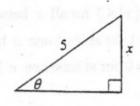
(E) It cannot be determined from the information given.



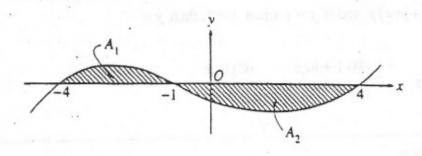
27. In the triangle shown on the right, if θ increases at a constant rate of 3 radians per minute, at what rate is x increasing in units per minute when x = 3 units?

(A) 3





28.



The graph of y = f(x) is shown in the figure above. If A_1 and A_2 are positive numbers that represent the areas of the shaded regions, then in terms of A_1 and A_2 , $\int_A f(x) dx - 2 \int_A f(x) dx =$

- (A) A,
- (B) $A_1 A_2$
- (C) $2A_1 A_2$
- (D) $A_1 + A_2$ (E) $A_1 + 2A_2$

- 29. Suppose that the function f has a continuous second derivative for all x, and that f(0) = 2, f'(0) = -3, and f''(0) = 0. Let g be a function whose derivative is given by $g'(x) = e^{-2x} (3f(x) + 2f'(x))$ for all x.
- (a) Write an equation of the line tangent to the graph of f at the point where x = 0.
- (b) Is there sufficient information to determine whether or not the graph of f has a point of inflection when x = 0? Explain your answer.
- (c) Given that g(0) = 4, write an equation of the line tangent to the graph of g at the point where x = 0.
- (d) Show that $g''(x) = e^{-2x} \left(-6f(x) f'(x) + 2f''(x)\right)$. Does g have a local maximum at x = 0? Justify your answer.
- 30. $\lim_{h \to 0} \frac{\ln(e+h)-1}{h}$ is
- (A) f'(e), where $f(x) = \ln x$ (B) f'(e), where $f(x) = \frac{\ln x}{x}$
- (C) f'(1), where $f(x) = \ln x$ (D) f'(1), where $f(x) = \ln(x+e)$
- (E) f'(0), where $f(x) = \ln x$
- 31. Let f be a continuous function on the closed interval [-3, 6]. If f(-3) = -1 and f(6) = 3, then the Intermediate Value Theorem guarantees that
- (A) f(0) = 0
- (B) $f'(c) = \frac{4}{9}$ for at least one c between -3 and 6
- (C) $-1 \le f(x) \le 3$ for all x between -3 and 6
- (D) f(c)=1 for at least one c between -3 and 6
- (E) f(c) = 0 for at least one c between -1 and 3
- 32. If $\frac{dy}{dx} = (1 + \ln x)y$ and if y = 1 when x = 1, then y =
- (A) $e^{\frac{x^2-1}{x^2}}$
- $(C) \ln x$
- (A) e^{x^2} (B) $1 + \ln x$ (D) $e^{2x + x \ln x 2}$ (E) $e^{x \ln x}$
- 33. $\int x^2 \sin x \, dx =$
- (A) $-x^2 \cos x 2x \sin x 2\cos x + C$ (B) $-x^2 \cos x + 2x \sin x 2\cos x + C$
- (C) $-x^2 \cos x + 2x \sin x + 2\cos x + C$ (D) $-\frac{x^3}{2} \cos x + C$

(E) $2x\cos x + C$