Date Name

Period

Worksheet 7.4—Vectors

Show all work on a separate sheet of paper. No Calculator unless otherwise specified.

Multiple Choice

- 1. Which of the following is the magnitude of the vector $\langle 2,-1 \rangle$?
- (A) 1 (B) $\sqrt{3}$ (C) $\frac{\sqrt{5}}{5}$ (D) $\sqrt{5}$
- (E) 5
- 2. Let $\vec{u} = \langle -2, 3 \rangle$ and $\vec{v} = \langle 4, -1 \rangle$. Which fo the following is equal to $\vec{u} \vec{v}$?

- (A) $\langle 6, -4 \rangle$ (B) $\langle 2, 2 \rangle$ (C) $\langle -2, 2 \rangle$ (D) $\langle -6, 2 \rangle$ (E) $\langle -6, 4 \rangle$
- 3. Which of the following represents the vector \vec{v} with a magnitude of 3 and a direction of 150°?

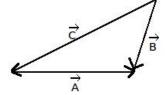
- (A) $\left\langle \frac{3\sqrt{3}}{2}, \frac{3}{2} \right\rangle$ (B) $\left\langle \frac{3}{2}, \frac{3\sqrt{3}}{2} \right\rangle$ (C) $\left\langle -\frac{3\sqrt{3}}{2}, \frac{3}{2} \right\rangle$ (D) $\left\langle -\frac{3}{2}, \frac{3\sqrt{3}}{2} \right\rangle$ (E) $\left\langle -\frac{3}{2}, -\frac{3\sqrt{3}}{2} \right\rangle$
- 4. Which of the following is a unit vector in the direction of $\vec{v} = -\vec{i} + 3\vec{j}$?

- (A) $-\frac{1}{10}\vec{i} + \frac{3}{10}\vec{j}$ (B) $\frac{1}{10}\vec{i} \frac{3}{10}\vec{j}$ (C) $-\frac{1}{\sqrt{10}}\vec{i} + \frac{3}{\sqrt{10}}\vec{j}$ (D) $\frac{1}{\sqrt{10}}\vec{i} \frac{3}{\sqrt{10}}\vec{j}$ (E) $-\frac{1}{\sqrt{8}}\vec{i} + \frac{3}{\sqrt{8}}\vec{j}$

- 5. Which of the following is a vector quantity?
 - (A) Energy
- (B) Power
- (C) Time
- (D) Force
- (E) Mass

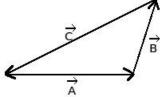
- 6. Which of the following is a scalar quantity?
 - (A) Area
- (B) Kinetic Energy (C) Weight of an object (D) Wind velocity
- (E) Acceleration
- 7. Which of the following gives the correct relation among the vectors in the diagram at right.

- (A) $\overrightarrow{A} + \overrightarrow{B} = \overrightarrow{C}$ (B) $\overrightarrow{B} + \overrightarrow{C} = \overrightarrow{A}$ (C) $\overrightarrow{C} + \overrightarrow{A} = \overrightarrow{B}$ (D) $\overrightarrow{A} + \overrightarrow{B} + \overrightarrow{C} = 0$



- 8. Which of the following gives the correct relation among the vectors in the diagram at right.
- (A) $\overline{A} + \overline{B} = \overline{C}$

- (B) $\overrightarrow{B} + \overrightarrow{C} = \overrightarrow{A}$ (C) $\overrightarrow{C} + \overrightarrow{A} = \overrightarrow{B}$ (D) $\overrightarrow{A} + \overrightarrow{B} + \overrightarrow{C} = 0$



- 9. A straight river flows west to east at a speed of 3 meters per minute. A man on the south bank of the river, capable of swimming at 6 meters per minute in still water, wants to swim across to the point directly opposite the bank. He should swim in a direction of
- (A) due north

- (B) 30° west of north (C) 30° east of north (D) 60° east of north
- (E) south

10. The angle between $\vec{i} + \vec{j}$ and \vec{i}

(A)
$$\frac{\pi}{6}$$

(B)
$$\frac{\pi}{4}$$

(C)
$$\frac{\pi}{3}$$

(D)
$$\frac{\pi}{2}$$

(A)
$$\frac{\pi}{6}$$
 (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{2}$ (E) $\frac{5\pi}{6}$

11. Consider a vector $\vec{F} = 4\vec{i} - 3\vec{j}$. The vector which is perpendicular to \vec{F} is

(A)
$$4\vec{i} + 3\vec{j}$$

(B)
$$-4\vec{i} + 3\vec{j}$$

(A)
$$4\vec{i} + 3\vec{j}$$
 (B) $-4\vec{i} + 3\vec{j}$ (C) $-3\vec{i} + 4\vec{j}$ (D) $3\vec{i} - 4\vec{j}$

(D)
$$3\vec{i} - 4\vec{j}$$

(E)
$$3\vec{i} + 4\vec{j}$$

12. The unit vector along $\vec{i} + \vec{j}$ is

(A)
$$\vec{i} + \vec{j}$$

(A)
$$\vec{i} + \vec{j}$$
 (B) $\frac{\sqrt{2}}{2}\vec{i} + \frac{\sqrt{2}}{2}\vec{j}$ (C) $\frac{1}{2}\vec{i} + \frac{1}{2}\vec{j}$ (D) $\sqrt{2}\vec{i} + \sqrt{2}\vec{j}$

(C)
$$\frac{1}{2}\vec{i} + \frac{1}{2}\vec{j}$$

(D)
$$\sqrt{2}\vec{i} + \sqrt{2}\vec{j}$$

(E) none of these

Short Answer

13. Show that \overline{AB} and \overline{CD} are equivalent by showing that they represent the same vector: A = (-4,7), B = (-1,5), C = (0,0), and D = (3,-2)

14. Given the points, A = (-2,2), B = (3,4), C = (-2,5), and D = (2,-8), find the indicated vector in $\vec{u} = \langle a, b \rangle$ chevron form, then find the magnitude, $|\vec{u}|$ of the vector.

(a)
$$\overline{BC}$$

(b)
$$4\overline{AC}$$

(b)
$$4\overline{AC}$$
 (c) $3\overline{BD} - 2\overline{AC}$

15. Given the vectors $\vec{u} = \langle 1, 3 \rangle$, $\vec{v} = \langle 2, 4 \rangle$, and $\vec{w} = \langle 2, -5 \rangle$, find the following vectors in \vec{i}, \vec{j} form. Find the magnitude of each new vector.

(a)
$$\vec{v} + \vec{w}$$

(a)
$$\vec{v} + \vec{w}$$
 (b) $-\vec{w} + \frac{1}{2}\vec{v}$ (c) $2\vec{u} - 3\vec{v}$

(c)
$$2\vec{u} - 3\vec{v}$$

16. Find a unit vector in the direction of $-2\vec{i}+3\vec{j}$. Write your answer in **both** chevron and \vec{i} , \vec{j} form.

17. Find the horizontal and vertical components of the vector with the given length and direction, then write the vector in \vec{i} , \vec{j} form.

(a)
$$|\vec{v}| = 50$$
, $\theta = \frac{7\pi}{6}$

(b)
$$|\vec{u}| = 13$$
, $\theta = 330^{\circ}$

(a)
$$|\vec{v}| = 50$$
, $\theta = \frac{7\pi}{6}$ (b) $|\vec{u}| = 13$, $\theta = 330^{\circ}$ (c) (Calculator) $|\vec{r}| = 900$, $\theta = 125^{\circ}$

18. Find the magnitude and direction (in degrees) of the following vectors.

(a)
$$\vec{u} = \left\langle -\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} \right\rangle$$
 (b) (Calculator) $\vec{v} = -9\vec{i} - 40\vec{j}$

19. (Calculator) Corny the jet pilot heads his jet due east. The jet has a speed of 440 mph relative to the air. The wind is blowing due north with a speed of 35 mph.

(a) Express the velocity of the wind as a vector in component form.

(b) Express the velocity of the jet relative to the air as a vector in component form.

(c) Find the true velocity of the jet as a vector.

(d) Find the true speed and direction of the jet.